Computational modeling of the passive and active components of the face

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Abstract

The face is probably the part of the body, which most distinguishes us as individuals. It plays a very important role in many functions, such as speech, mastication, and expression of emotion. In the face, there is a tight coupling between different complex structures, such as skin, fat, muscle, and bone. Biomechanically driven models of the face provide an opportunity to gain insight into how these different facial components interact. The benefits of this insight are manifold, including improved maxillofacial surgical planning, better understanding of speech mechanics, and more realistic facial animations. This chapter provides an overview of facial anatomy followed by a review of previous computational models of the face. These models include facial tissue constitutive relationships, facial muscle models, and finite element models. We also detail our efforts to develop novel general and subject-specific models. We present key results from simulations that highlight the realism of the face models.

Keywords: Face, finite element models, constitutive relationships, skin, muscles, expressions, lips

Introduction

The development of computational face models is motivated by their application in many disciplines, including animation, biomedical engineering, and forensics [17, 68, 70]. Clinical uses of face models could also improve patient outcome.

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While face animation has been used for realistic talking heads for computational social agents [54], the technique still does not cross the uncanny valley. This phenomenon proposes that as artificial faces become more realistic they become more eerie and repulsive to a perceiver [44]. Facial animations fail to cross the uncanny valley partly due to the unrealistic motion of the facial tissue. However, biomechanically driven models, such as finite element models, of the face provide the opportunity to incorporate the subtleties of how facial skin and the underlying layers move physically. Furthermore, when combined with biomechancially based models, such as the upper airway (chapter 10), and tongue (chapter 25), it is possible to have a complete functional model of a talking, breathing, and eating head that captures the underlying physics of motion during these complex movements leading to a more realistic correlation between form and function needed to cross the uncanny valley. These biomechanical face models can also be used for maxillofacial surgical simulations [31] to facilitate planning and training of complex operations to improve speech and mastication outcomes [62]. Additionally, realistic face prosthetics can be designed to move and deform realistically using these face models [36].

We can use simulations to investigate speech mechanics. Jaw, lip, and tongue coordination for speech is challenging to analyse experimentally. Physically accurate face models can compliment experiments and help determine clinical solutions to patients' speech impediments [59].

Background

The human face comprises many anatomical components that contribute to appearance and function. Several accounts describe facial anatomy [34, 51]. Briefly, we summarise the structures in layers from superficial to deep.

Skin

Skin forms the outer face layer and contains the outer epidermis and the underlying dermis. The epidermis contains several cell layers. The dermis comprises collagen and elastin fibres embedded in a ground matrix. Facial skin thickness and composition varies according to position and person. Its thickness ranges from 0.5 mm on eyelids to 1.5 mm on cheeks [35, 48, 66].

Subcutaneous fat

Under the skin, the face contains several superficial fat compartments. They are the nasolabial fat compartment; temporal-cheek fat pads, which cover the cervical, cheek, and forehead regions; orbital fat pads; and the jowl fat compartment in the lower third of the face. Each compartment

is separated by fascial tissue and septae [51]. With aging, volume loss occurs at different rates in the fat compartments, which leads to less smooth contours on facial surfaces.

$Superficial\ musculoaponeurotic\ system$

The superficial musculoaponeurotic system (SMAS) is a tissue sheet of collagen and elastin fibres, and fat cells extending from the neck up to the forehead [43]. It plays a key role in facial expression by connecting mimetic muscles to the dermis.

Two SMAS types exist. Type I SMAS occurs in the forehead, parotid, zygomatic, and infraorbital areas and comprises fibrous septae. Type II SMAS is a dense mesh of collagen, elastin, and muscle fibres and is found in the lip area [28]. SMAS thicknesses vary throughout the face from 2 mm to 3 mm [32].

Retaining ligaments

Retaining ligaments are fibrous connective tissue condensations that either anchor skin to bone (also known as true retaining ligaments) or soft tissue layers to each other (also known as false retaining ligaments). The zygomatic ligament anchors the dermis near the inferior border of the zygomatic arch. The mandibular retaining ligament connects mandibular bone to the dermis. The orbicularis retaining ligament anchors the dermis in the anterior orbital rim region [42]. False retaining ligaments include the masseteric and platysma-auricular ligaments. The masseteric ligament is positioned along the anterior masseter muscle border and connects the SMAS and dermis. With aging, the retaining ligaments become weaker, which results in tissue sagging [42].

Mimetic muscles

Beneath the layer of retaining ligaments are numerous thin flat muscles known as mimetic muscles (figure 24.1). In the eye region are five muscle sets: the frontalis is the main elevator of brows; corrugator supercilli also depress brows and cause them to move medially; depressor supercilli have similar functions; obicularis oculi cause eyes to squeeze shut; and procerus pull lower forehead skin down to cause a horizontal crease on the nose [51].

Around the mouth are levator muscles, zygomaticus major and minor, risorius, buccinator, orbicularis oris, depressor anguli oris, depressor labii, and mentalis. Zygomaticus major and minor originate in the zygomatic bone and insert in the mouth corner to lift it. The levator muscles (labii, labii superioris alaeque nasi, and anguli oris) elevate the upper lip and mouth corner. The risorius extends from the lateral cheek and inserts into the mouth corner, pulling it

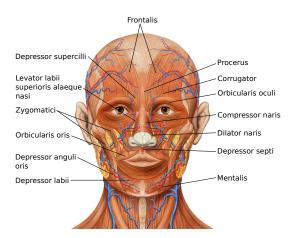


Figure 24.1: Face muscles. Note that the buccinator and risorius muscles are not indicated in this sketch. From [40]. Adapted under licence.

laterally. It is absent from some people [4]. The buccinator pulls back on the mouth and flattens the cheek. The orbicularis oris is a sphincter around the mouth responsible for lip action. Depressor anguli oris originates in the mandible and merges with orbiculoris oris depressing the mouth corners upon contraction. Depressor labil inferioris arises from the mandible and extends upwards into the lower lip. Medial to this muscle is the mentalis, which elevates and protrudes the lower lip.

In the nose region, the compressor naris compresses the nasal passage; the dilator naris dilates the nostrils; and the depressor septi moves the nose tip downwards.

Twenty mimetic muscles have to be modelled to represent the whole face [68]. The models presented in later sections model a subset of these muscles to simulate specific facial expressions.

Deep-plane fat

In the deep plane beneath the mimetic muscles lie the suborbicularis oculi, bucal, and galeal fat pads. As well as providing volume and shape to the face, they act as glide planes for free movement of facial muscles. In particular, the suborbicularis oculi fat pad lies underneath the orbicularis region. The bucal fat pad allows movement of the mastication muscles. The corrugator and procerus glide upon the galeal fat pad. Deep plane fat pad volume loss occurs with ageing resulting in visible folds and grooves.

Facial skeleton

The skeleton provides anchoring points for muscles and structural support for facial soft tissues. The main facial bones are the frontal, zygomatic, maxilla, nasal, and mandible bones.

Previous computational models of the face

Facial tissue constitutive relationships

Constitutive facial soft tissue model development has been ongoing for several decades [5, 27, 52, 53]. Many models were developed to simulate soft tissue from other anatomical locations.

Validating constitutive models requires experimental data. There is a relative dearth of such data to determine material parameters for facial soft tissues. Many studies use the Cutometer[®] (Courage and Khazaka Electronic GmbH, Köln, Germany), which applies suction to skin [15, 49, 61], enabling parameters characterising skin distension and retraction to be identified. These studies demonstrate how age influences facial skin mechanical response [16] and property variations from person to person [39]. The format of reported results are not ideal for constitutive model development with certain skin deformation measurements only detailed at a couple of specific times. Other studies using similar suction protocols include Barbarino et al. [5] and Luboz et al. [38]. A variation on this approach is to blow air normal to facial skin [25]. These approaches cannot characterise anisotropic properties of facial tissues due to axi-symmetrical loading.

Ohshima et al. [49] used a Reviscometer[®] (Courage and Khazaka Electronic GmbH, Köln, Germany) to characterise anisotropic properties of three areas on 91 female faces. The approach assumes a linear stress-strain response by relating the wave speed and Young's modulus of skin.

A constitutive model developed to characterise facial tissue anisotropic dissipative response is detailed in work by Rubin and Bodner [52]. This model further develops the approached published in Rubin et al. [53] and represents tissue as a composite of an elastic fibre component and a dissipative component. The strain energy equation is

$$W = \frac{\mu_0}{2q}(e^{qg} - 1), \qquad g = g_1(J) + g_2(\bar{\mathbf{B}}) + g_3(\lambda_1) + g_4(\alpha_1), \tag{1}$$

where μ_0 is a material constant having the units of stress and q is a dimensionless constant that controls the nonlinearity of the moduli. J is the volume ratio, and $\bar{\mathbf{B}}$ is the deviatoric left Cauchy tensor. λ_1 represents the fibre stretch, and $\alpha_1 = \bar{\mathbf{B}}_{de} \cdot \mathbf{I}$, where $\bar{\mathbf{B}}_{de}$ is a pure measure of elastic distortional deformation associated with the dissipative component. g_1 characterises volume dilation; g_2 characterises total distortion; g_3 accounts for fibre stretch; and g_4 represents distortional dissipative deformation.

$$g_1(J) = 2m_1[(J-1) - \ln(J)]$$

$$g_2(\mathbf{\bar{B}}) = m_2(\mathbf{\bar{B}} : \mathbf{I} - 3)$$

$$g_3(\lambda_1) = \frac{m_3}{m_4} \langle \lambda_1 - 1 \rangle^{2m_4}$$

$$g_4(\alpha_1) = \alpha_1 - 3,$$
 (2)

where m_{1-3} are dimensionless material parameters related to the response of dilation, distortion, and fibre stretching. m_4 is a dimensionless constant that controls the nonlinearity of the response to fibre stretching. The McAuley brackets $\langle \bullet \rangle = (|\bullet| + \bullet)/2$ ensure no resistance to compression in fibres.

Rubin and Bodner [52] evaluated the ability of this strain energy equation to simulate uniaxial tension of in vitro facial skin and SMAS [32]. While the experimental data was insufficient for simulating tissue anisotropy, the model did simulate the cyclic loading-unloading and stress relaxation response of the samples.

A simplified Rubin-Bodner model has been used in studies on facial tissue mechanics. Barbarino et al. [5] ignored the fibres and dissipation contributions when characterising five facial points ($g_3 = g_4 = 0$ in equation (2)), reducing the parameter number from fourteen to three independent parameters with physical meaning. $\mu_0 m_1$ represents the initial bulk modulus, $\mu_0 m_2$ represents the initial shear modulus, and qm_2 represents the nonlinearity of the moduli.

Barbarino et al. [5] also fit a second-order reduced polynomial equation to the average response from the five facial points.

$$W = C_{10}(I_1 - 3) + C_{20}(I_1 - 3)^2 + \frac{1}{D_1}(J - 1) + \frac{1}{D_2}(J - 1)^2,$$
(3)

where C_{10} , C_{20} , D_1 , and D_2 are material parameters, and $I_1 = \mathbf{\bar{B}} \cdot \mathbf{I}$.

They chose this model because it is commonly implemented in commercial finite element software.

They used a Cutometer[®] and an aspiration device to get measurements in five facial regions - the forehead, zygomatic, parotid, nasolabial, and jaw. The 2 mm diameter aperture on the Cutometer[®] was used to characterise the superficial skin layer. The larger 8 mm aperture on the aspiration device deformed the deeper layers to characterise the SMAS and fat layers. They developed an axisymmetric finite element model consisting of a 1.7 mm thick skin layer and a 3 mm layer representing both the SMAS and fat. They identified material parameters that best-fit the Rubin-Bodner model and the second order reduced polynomial model to the averaged response of the five facial points.

Weickenmeier et al. [64] developed this approach further by including the dissipative component of the Rubin-Bodner model ($g_4 \neq 0$ in Equation (2)). Using a similar protocol to Barbarino et al. [5] and an axi-symmetric finite element (FE) model, they determined in vivo material parameters that simulated the averaged response of three facial points (forehead, parotid, and jaw). Differences occurred in some material parameter values between Weickenmeier et al. [64] and both Barbarino et al. [5] and Rubin and Bodner [52]. These differences are explained by the in vitro samples used in Rubin and Bodner [52] and ignoring dissipative effects in Barbarino et al. [5].

The simplified Rubin-Bodner models used in Barbarino et al. [5] and Weickenmeier et al. [64] ignored in vivo facial skin anisotropic properties. Flynn et al. [22] used a force-sensitive micro-robotic device to apply a rich deformation set to facial skin of five volunteers. In all cases, a nonlinear, anisotropic, and viscoelastic force-displacement response was recorded. They proposed a simplified FE model, with a second-order Ogden strain energy equation and a quasi-linear viscoelastic relationship representing skin.

$$W = \sum_{i=1}^{2} \frac{\mu_i}{\alpha_i} (\lambda_1^{\alpha_i} + \lambda_2^{\alpha_i} + \lambda_3^{\alpha_i}) + \frac{1}{d_i} (J - 1)^2, \tag{4}$$

where μ_i is a material parameter with dimensions of stress and α_i is a parameter controlling the nonlinearity of the response. d_i is the bulk modulus. λ_1 , λ_2 , and λ_3 are the principal stretches.

$$\mathbf{T}(t) = \mathbf{T}_e(t) + \int_0^t \mathbf{T}_e(t - \tau) \frac{\partial g_R(\tau)}{\partial \tau} d\tau, \tag{5}$$

where $\mathbf{T}(t)$ is the total Cauchy stress tensor at t, \mathbf{T}_e is the elastic Cauchy stress tensor, $g_R(t) = 1 - \bar{g}_1^P (1 - e^{-t/\tau_1^G})$ is the reduced relaxation function represented by a Prony series. \bar{g}_1^P is a viscoelastic parameter and τ_1^G is the relaxation time.

In-plane pre-stresses in two orthogonal directions were also applied to simulate the tension in living skin. Nonlinear optimisations generated material parameters and in vivo pre-stresses that best-fit the central cheek response of five volunteers and several points of one volunteer.

Recently, Flynn et al. [23] simulated the same data set using an anisotropic constitutive model [26].

$$W = \frac{\mu}{2}(I_1 - 1) + \frac{k_1}{k_2} \{ e^{k_2[\bar{I}_n(\theta) - 1]^2} - 1 \},$$
 (6)

where μ and k_1 control the stiffness of the material at low strains, and k_2 is a dimensionless parameter that controls the stiffness of the material at high strains. $\tilde{I}_n(\theta) = \mathbf{N}\bar{\mathbf{C}}\mathbf{N}$ is the

fibre stretch squared of the nth family of fibres orientated in the direction \mathbf{N} in the reference configuration. $\mathbf{\bar{C}}$ is the deviatoric right Cauchy tensor.

The finite element model in the study was based on a single layer of shell elements. The constitutive relationship has previously been used to simulate the response of in vitro skin under uniaxial tension Annaidh et al. [2]. The error between model and experiment was less than the error reported by Flynn et al. [22]. This is expected with the use of a constitutive relationship that more accurately represents the fibre orientation than an isotropic relationship.

Facial muscle modelling

Facial muscles are striated compared to soft muscles, and activation induces contraction along fibres. Muscle simulations should include fibre directions and a model to generate contractions.

Fibre directions in face models are generated manually using anatomical data or fitting B-splines on digitized fibre directions through a serial dissection of the muscle [33, 56, 67].

In FE models, muscle fibres can be aligned along element edges. The muscle force is a function of length and velocity difference between element edge nodes [10]. Fibres are also represented using link elements and using temperature to model activation. This approach models passive muscle stiffening [45, 46].

Transversely isotropic relationships represent muscle passive properties [57]. The strain energy derivative with respect to the invariant $I_4 = \mathbf{a}_0 \mathbf{C} \mathbf{a}_0$ gives the stress along the fibres. \mathbf{a}_0 is the unit vector along the initial fibre direction and \mathbf{C} is the right Cauchy-Green strain tensor. Adding this stress to the active muscle stress gives the total stress in the contracting muscle.

Muscle force generation models are typically of the Hill-type with the muscle force generated, F_{ce} , given by

$$F_{ce} = F_{max}F(l,v)f_A \tag{7}$$

where F_{max} is the maximum muscle force generated, $F(l,v) = f_l g(v)$ (with f_l being the tension-length and g(v) being the tension-velocity muscle characteristics), and f_A represents activation dynamics from the central nervous system [69].

An alternative to Hill-type models is Feldman's λ model [18]. Both approaches differ in two ways. Firstly, in a Hill-type model, muscle force is controlled by the maximum force variable. In the λ model, muscle force is a consequence of the combination of the stretch reflex and the force-length characteristic of the muscle. Secondly, to assign values to the parameters of Hill-type models, experimental data is needed when the muscle is maximally activated. The λ model is

based on experimental data from unloading tasks. The generated muscle force in the λ model is

$$F_{ce} = F_{max}F(A, l, v, d, t)g(v)$$
(8)

where A is the muscle threshold length, d is the reflex delay. The current muscle force is dependent on the length and velocity at time t. This model simulates the nonlinear force-stiffness of muscles (see figure 6.5 in McMahon [41]).

Overy et al. [50] showed the λ model had a more realistic response rate compared to the Hill-type model. In a study of orofacial gestures, no clear biomechanical differences were found between the two models [47].

Finite element models

Early physically-based face models considered the face as a mass-spring lumped parameter system [60]. Models since then have used FE methods to simulate the nonlinear finite deformations that facial tissues undergo.

Sifakis et al. [56] developed a FE model with a rigid surface mesh for bone, a tetrahedral mesh for soft tissue, and embedded vectors representing muscle fibres. A Mooney-Rivlin equation represented the soft tissue. They simulated facial expressions and narration sequences and determined muscle activations that best-fit model surface-points to corresponding experimentally tracked surface markers for a given action. Gladilin et al. [30] developed a FE model for craniofacial surgery applications. It comprised a linear elastic soft tissue mesh (Young's modulus 2.2 MPa, Poisson's ratio 0.45) and muscles represented virtually by a vector field inside a 3-D ellipsoid. Pre-computed muscle forces simulated happiness and disgust. Beldie et al. [7] simulated facial expressions pre and post maxillofacial surgery. The model contained rigid bone, skin, fat tissue, and 20 facial muscles. The latter were represented using a Hill-type muscle model. A linear elastic model represented skin (Young's modulus 15 kPa, Poisson's ratio 0.49) and a neo-Hookean material represented the fat ($C_{10} = 420 \text{ Pa}$, Poisson's ratio of 0.495).

Chabanas et al. [13] developed several patient-specific models to simulate mandible repositioning. They divided the soft tissue into two layers representing the dermis and hypodermis, which were simulated using a linear-elastic model (Young's modulus 15 kPa, Poisson's ratio 0.49). Barbarino et al. [4] developed a very detailed FE model based on MRI data. The skull and mandible were represented along with retaining ligaments, skin, a combined SMAS and hypodermis layer, and deeper subcutaneous tissue. Eleven passive facial muscles were present. The simplified Rubin-Bodner model (Equations (1) and (2)) was used to represent soft tissues. They

modelled the insertion of a rigid ball inside the oral cavity between the teeth and cheek. They also simulated ageing by reducing tissue stiffness.

Another detailed face model has been presented by Wu et al. [68]. Their cubic-hermite FE model comprised a combined skin, subcutaneous and SMAS layer, and an underlying deep fascia layer. Twenty transversely-isotropic muscle pairs were embedded in the mesh to simulate facial expressions. Soft tissues and passive muscle properties were represented by a Mooney-Rivlin equation ($C_{10} = 0.42 \text{ kPa} - 2.50 \text{ kPa}$; $C_{20} = 0.0 \text{ kPa} - 1.175 \text{ kPa}$). The deep fascia layer was considered as a rigid surface mesh and the superficial layer glided upon it. The authors found more realistic expressions resulted from this glide-plane. They evaluated four simulated facial expressions by comparing surface data with measurements obtained using a 3D structured-light scanner. The largest differences occurred in the lip region.

Recently, Warburton and Maddock [63] presented an explicit finite element forehead model comprising stratum corneum, dermis, and hypodermis. The frontalis, procerus, and corrugator supercilli muscles were also present. Soft tissue components were represented by a neo-Hookean model ($C_{10} = 0.034 \text{ MPa} - 48 \text{ MPa}$ depending on the tissue). The active and passive components of the transversely isotropic were summed. The model efficiently simulated soft tissue sliding over the skull and created physically-realistic wrinkles.

Many of the FE models described accurately represent the geometric characteristics of the hard and soft tissues. However, several simplifying assumptions are made with respect to the mechanical properties of the soft tissues. Several models assume the skin to be an isotropic material Barbarino et al. [4], Sifakis et al. [56], Warburton and Maddock [63], and Wu et al. [68]. Others assume skin to have a linear stress-strain response Beldie et al. [7], Chabanas et al. [13], and Gladilin et al. [30]. None of the previously described models consider the tension inherent in living skin, which plays an important role in wrinkling Flynn and McCormack [20] and influences the design of surgical incisions Borges [9]. To make useful predictions from biomechanical face models, it is important to represent skin as an anisotropic, nonlinear material under tension. The stiffening effect of muscles when under stress is also not accounted for in previous face models. It is proposed that this effect plays a vital role in lip shaping, which has consequences for speech mechanics.

The remainder of this chapter describes our efforts to develop face models that contains an anisotropic skin model with pre-stress and includes muscles that stiffen under stress.

Face model development

General face model

The first face model was created using a patient's CT scans by generating the skin and skull surfaces respectively using the method described in Chabanas et al. [13]. The volume between, representing the facial tissue, was meshed manually to create three different layers with hexahedral and wedge elements [46]. The model was developed within ANSYS (ANSYS, Inc., Cecil Township, PA, USA) and contained 6030 hexahedral elements, 314 wedge elements, and 8736 nodes (figure 24.2). The wedge element formulation is a degenerated formulation from the hexahedral formulation. The mesh was created symmetrically with respect to mid-sagittal plane

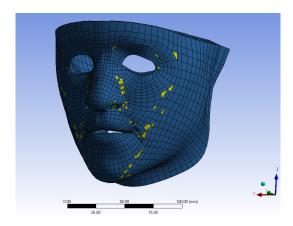


Figure 24.2: General face model: wedge elements are yellow and hexahedral elements are blue; From Nazari et al. [45]. Copyright 2011 by Human Kinetics. Adapted with permission.

to reduce the number of degrees of freedom and thus reduce the computational time. We defined contact elements between upper and lower lips and between the lips and a surface simulating teeth. Attachment nodes on the skull were fixed. We defined muscle pathways with the help of anatomical data and CT scans. Muscles were defined as cable elements, which act in tension only. End points of the cable elements correspond to anatomical landmarks located in reference to the skull. This means that their definition is independent of the refinement of the soft tissue mesh. Point to surface contact elements coupled the cable elements with the main mesh. The end points of the cable elements are coupled to the surface of mesh elements whose centroid is closest to the cable extremity. A volume running along each cable element line with a radius equal to the muscle cross-sectional dimension is determined. Elements of the main mesh intersecting this volume is then labelled as a part of the muscle body. Simulations creating different facial

gestures were produced. For a detailed discussion see Nazari et al. [46]. In Nazari et al. [45] the model's behaviour was verified as a first model producing lip protrusion and lip rounding. This model was used as a basis to create a patient specific model using mesh morphing operations [11, 12].

Subject-specific model development

Finite element model

Starting from the finite element mesh developed with ANSYS, this model was further developed within Artisynth (www.artisynth.org), an open source biomechanical modelling platform developed at the University of British Columbia (figure 24.3) [37].

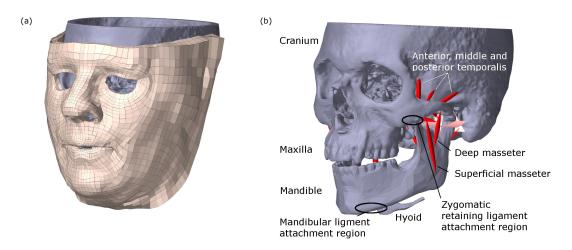


Figure 24.3: Subject-specific face model: (a) soft tissue mesh; (b) bones, jaw muscles, and ligament attachment points; From Flynn et al. [24]. Copyright 2015 by Taylor & Francis Ltd. Adapted with permission.

The cranium, maxilla, and hyoid are represented as rigid bodies and fixed in space. The jaw is connected to the hyoid and muscles represented as point-to-point Hill-type actuators [58].

A finite element mesh, similar to that discussed in the previous section, represents soft tissue. The outer and inner mesh surfaces were fit to corresponding surfaces of CT data of an adult male [12]. The mesh has three element layers with the outer element layer representing skin, and inside layers representing the hypodermis.

We implemented the mimetic muscles in the same manner as described in the previous section (figure 24.4). Elements in the path of a muscle are assigned passive and active properties. The total muscle fibre response is based on a transverse-isotropic relationship proposed by Blemker et al. [8]. The passive stress along the fibres increased exponentially with increasing fibre stretch

[65]. This results in a stress stiffening effect. The same muscle material parameters were used. $\lambda^* = 1.4$ is the stretch at which the fibres are straightened, $P_3 = 0.05$ scales the exponential stresses, and $P_4 = 6.6$ is the rate of uncrimping of fibres. The maximum active fibre stress was 100 kPa.

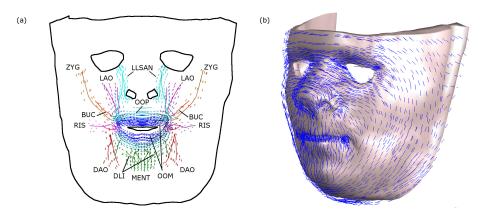


Figure 24.4: (a) Orofacial muscles including element muscle fibres; (b) relaxed skin tension line direction assigned to each element; From Flynn et al. [24]. Copyright 2015 by Taylor & Francis Ltd. Adapted with permission.

The zygomatic ligaments are represented by fixing the nodes in the soft tissue mesh closest to the region where these ligaments attach to the maxilla. Soft tissue nodes in the mandibular ligament attachment regions are fixed to the mandible.

Contact between soft tissue and bony structures is modelled, along with contact between upper and lower lip surfaces. Contact is based on interpenetration of the surface nodes. Velocity constraints are formed between interpenetrating nodes and opposing faces. The direction of the constraint is the normal of the opposing face closest to the interpenetrating node. These constraints are added to the system in subsequent time-steps to correct the interpenetration.

Soft-tissue constitutive equations

The hypodermis is represented by a Mooney-Rivlin constitutive equation.

$$W = C_{10}(\bar{I}_1 - 3) + C_{20}(\bar{I}_1 - 3)^2 + \frac{\kappa}{2}(\ln J)^2, \tag{9}$$

where $C_{10} = 0.4$ kPa, $C_{20} = 1.4$ kPa, and $\kappa = 50$ kPa are material parameters taken from [5].

We used a frame-invariant Fung constitutive equation for the skin [3].

$$W = \frac{c}{2}(e^{Q} - 1) + \frac{\kappa}{2}(\ln J)^{2},\tag{10}$$

$$Q = c^{-1} \sum_{a=1}^{3} \left[2\mu_a \mathbf{A}_a^0 : \bar{\mathbf{E}}^2 + \sum_{b=1}^{3} \lambda_{ab} (\mathbf{A}_a^0 : \bar{\mathbf{E}}) (\mathbf{A}_b^0 : \bar{\mathbf{E}}) \right], \tag{11}$$

where c, μ_a , λ_{ab} are material parameters whose values are based on in vivo tests on forearm skin [21] (table 1).

Table 1: Material parameters for different skin-types. TSF stands for Tension Scale Factor. From [24]. Copyright by Taylor & Francis Ltd. Adapted with permission.

Skin type	c (kPa)	$\mu_1(kPa)$	$\mu_2 \text{ (kPa)}$	μ_3 (kPa)	$\lambda_{11} \; (\mathrm{kPa})$	$\lambda_{22} \; (\mathrm{kPa})$	TSF
Normal	21.3	17.8	5.9	5.9	1.0	1.0	1.10
Stiff	42.6	35.6	11.8	11.8	11.8	2.0	1.05
Soft	10.7	8.9	3.0	3.0	0.5	0.5	1.15

 $\bar{\mathbf{E}} = (\bar{\mathbf{F}}^T \bar{\mathbf{F}} - \mathbf{I})$ is the distortional Green-Lagrange strain tensor; $\mathbf{A}_a^0 = \mathbf{a}_a^0 \otimes \mathbf{a}_a^0$, where \mathbf{a}_a^0 defines an initial material axis direction a. For each soft tissue element, \mathbf{a}_a^0 was set to the relaxed skin tension line direction in that region (figure 24.4(a)) [9].

Implementing skin pre-stress

A novel aspect of Flynn et al. [24] is the pre-stress in the soft tissue mesh. Prior to the FE analysis, all the nodal coordinates of the soft tissue mesh were scaled by dividing by a tension scale factor (TSF). At the start of the FE analysis, the globally-scaled soft-tissue mesh corresponded to the stress-free configuration. During the initial analysis step, displacement boundary conditions were imposed on all nodes of the inner surface of the soft-tissue mesh. These boundary conditions transformed these inner nodes back to their original reference positions. Any nodes on the inner surface, which were not attached to bony structures or ligaments, had their displacement boundary conditions removed. In place of these boundary conditions, the corresponding reaction forces were imposed. These reaction forces were reduced linearly to zero in 1 second. This was a more stable procedure than suddenly releasing the nodes. These operations created a pre-stress in the soft tissue. Three different TSFs were analysed. With a TSF=1.05, the pre-stress in the skin mesh averaged 2.5 kPa. A TSF=1.1 resulted in pre-stresses of 5.2 kPa and a TSF=1.15 resulted in pre-stresses of 9.9 kPa. The values of TSF were chosen to give pre-stress levels within estimated in vivo ranges.

Model evaluation

We evaluated the model by simulating several actions and comparing landmark displacements and distances between certain landmark pairs with corresponding in vivo measurements (figure 24.5(a)). Details of the experimental protocols can be found in Coulson et al. [14], Giovanoli et al. [29], and Sforza et al. [55]. We simulated facial expressions by activating appropriate facial muscle sets (see Table 1 in [24]). These expressions included open-mouth smile, closed-mouth smile, pursing of lips, and lips turned downwards. Activation levels were chosen that resulted in realistic expressions. Wide mouth opening was simulated by activating the pterygoid and digastric muscles with 100% activation in each [58].

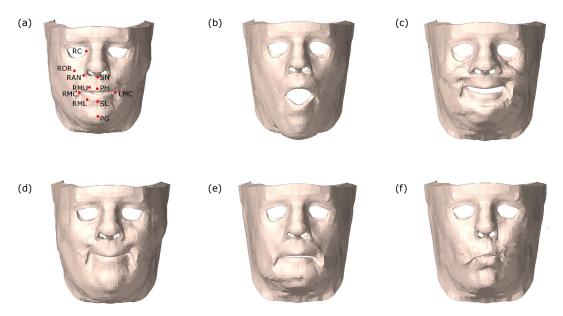


Figure 24.5: (a) Facial landmarks; (b) Wide open mouth; (c) open-mouth smile; (d) closed-mouth smile; (e) lips turned downwards; (f) lips pursed. From Flynn et al. [24]. Copyright 2015 by Taylor & Francis Ltd. Adapted with permission.

We also investigated skin stiffness and pre-stress effects on landmark displacements during facial actions (table 1). These skin properties changes are similar to what is observed in ageing skin [1, 6].

Results

General face model results

Different facial gestures were produced by activating appropriate muscles in the general face model. The resulting gestures are consistent with those produced by the corresponding muscles reported in the anatomical references. The computational time for each simulation was about 35 minutes on a 2.6GHz Core 2 Duo processor.

Focusing on lip protrusion and lip rounding, better lip shaping occurs when we stiffen facial tissues [46] (figure 24.6). This is due to the stress stiffening effect of muscle fibres when they generate contraction forces along their length. In early model versions, fibre numbers were small (maximum two per muscle). The stiffening effect was introduced in the model through the change of passive properties during activation (the coefficients in Mooney-Rivlin hyperelastic model).

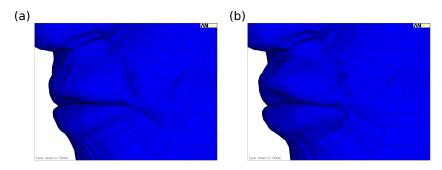


Figure 24.6: The effect of orbicularis oris muscle activation: (a) with stress stiffening, a more real-sitic effect occurs; (b) with no stress stiffening, the lips protrude excessively.

Subject-specific model results

Displacement of inner soft tissue mesh nodes from their scaled positions to the reference subject position created a tension field where the direction of maximum tension in any region was similar to relaxed skin tension lines observed by Borges [9]. When the mouth was wide open, the directions of maximum tension changed in-plane by up to 90° in the chin and anterior mandible regions. For an open-mouth smile, the cheek area experienced the largest tension direction changes [24].

Activating appropriate muscles generated different facial expressions (figure 24.5(b)-(f)). For all facial expressions, the mouth corner displaced the most, as observed experimentally [14, 29, 55]. For "normal" skin with a 10% TSF, model landmark displacements were within a standard deviation of experimental measurements (figure 24.7). Ferrario and Sforza [19] reported errors

in the method of Sforza et al. [55] ranging from 0.5-3.38 mm. In general, increasing skin stiffness resulted in smaller landmark displacements during facial expression. Increasing tension in the soft tissue had a variable effect on landmark displacements. When smiling, central upper lip displacement increased with increasing tension but decreased with increasing tension when lips pursed or turned downwards.

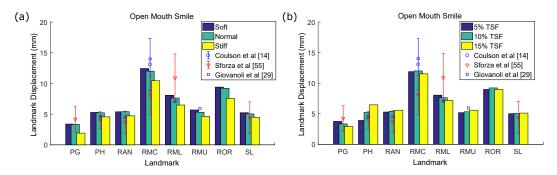


Figure 24.7: Variation of landmark displacements for skin with different (a) stiffnesses with a TSF of 10%; (b) tensions with a normal skin stiffness. Standard deviations are reported from [14, 29, 55]. From Flynn et al. [24]. Copyright 2015 by Taylor & Francis Ltd. Adapted with permission.

Conclusion

Creating physically-realistic facial simulations requires us to overcome several engineering challenges. There are many complex interactions between hard and soft tissues. Most materials are nonlinear, anisotropic, and time-dependent. Simulating how muscles drive facial expressions is a difficult undertaking. There are diverse benefits to overcoming these challenges, such as improved maxillofacial surgical planning, better insights into speech production, and superior animation quality.

In this chapter, we have outlined several computational tissue, muscle, and full face models in the literature. We have also demonstrated our approach for simulating human facial expressions. Results from the models have indicated good agreement with experimental measurements. The addition of an orthotropic constitutive equation to represent skin and the implementation of a pre-stress are advancements over previous models. Accounting for the stress-stiffening effect in muscles, which has not been considered in earlier models, results in more realistic deformations, especially in the lip region.

There is much work to do to advance the state of the art. More efficient computational techniques are needed to increase the simulation speed. This would increase their usefulness

to predict patient outcome from maxillofacial surgery. Additional soft-tissue characterisation of specific facial regions will improve model behaviour. Measuring mimetic muscle activations during facial expressions and lip movements will inform the face model. A limitation is that the finite element model of the face does not correspond to any of the faces used for the in vivo landmark measurements. Realistic connections between soft-tissue layers and between soft and bony structures needs to be implemented.

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